

# Reactive Temporal Logic Planning for Safe Human-Robot Interaction

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**Abstract**—Human-robot interaction plays a critical role in scientific experiments by ensuring efficient and reliable execution of experimental tasks. To achieve successful task completion, robots must adapt in real time to unexpected task variations, external disturbances, and safety constraints. In this work, we propose a reactive task and motion planning framework designed to address these challenges. By formulating interaction tasks using Linear Temporal Logic (LTL), our approach introduces Planning Decision Tree and Augmented Planning Decision Tree approach to dynamically adjust task sequences in response to environmental changes. At the execution layer, we employ a Model Predictive Path Integral controller, which ensures both efficient and safe control. Additionally, the planning interface effectively coordinates the planning and execution layers, ensuring strict adherence to experimental task specifications. The effectiveness of the proposed reactive planning framework is demonstrated through physical experiments using a 7-DoFs robot. Project website: <https://sites.google.com/view/rtlp-iros/>

## I. INTRODUCTION

In scientific experiments [1], [2], the integration of robotic systems as carriers, combined with human-robot interaction, has emerged as a novel research paradigm. A critical challenge in this domain is ensuring experimental safety and adherence to procedural standards while enabling robots to effectively manage the dynamic uncertainties inherent in human-robot interactions. Specifically, robots must accurately adjust task planning and control strategies to maintain flexibility in response to environmental variations. In human-robot interaction scenarios, robots must strictly adhere to temporal logic constraints to successfully execute designated experimental tasks. Any deviation from these constraints during task execution can lead to significant operational failures and severe consequences. Additionally, human operators may dynamically introduce temporary tasks based on experimental progress, requiring the robot to resolve potential conflicts between global and local temporary task objectives while ensuring adherence to safety constraints.

To deal with task changes, in [2], a time-varying cost function was designed to adjust task priorities in response to changes. However, this approach is suboptimal when handling randomly triggered tasks, as it necessitates manually predefined and complex state transition relationships. Furthermore, due to the rapid expansion of the symbol space, PDDL solvers cannot guarantee the system's real-time responsiveness. Alternative approaches, such as those

in [3]–[5], leverage behavior trees, observation updates, and free-energy minimization to adapt to unforeseen local actions and resolve task conflicts. However, these methods depend on precise estimations of the robot's belief state, which is often impractical in real-world applications.

The rich expressiveness of Linear Temporal Logic (LTL) makes it a widely utilized framework for specifying complex robotic tasks [6]–[11]. LTL-based reactive planning algorithms dynamically adapt task execution in response to environmental and task variations, ensuring robust system performance across diverse conditions [12]–[22]. When responding to transient dynamic events [12], [15], the robot must accurately assess the current task progress to ensure continuous task advancement [18], [19], [23]. Sampling-based methods require searching for solutions over the product of Büchi automata and the transition system [7], which imposes significant computational overhead. Prior works [12], [13] have demonstrated the capability to manage localized single tasks in dynamic environments; however, they struggle with scenarios where local tasks are interdependent with global task objectives. A reconfigurable planning approach based on behavior trees [15] enables robots to adapt and plan with minimal replanning steps by leveraging past experiences. However, this method relies on the cross-product of states and automata, which significantly constrains search efficiency when handling complex local task specifications. Reactive synthesis and probabilistic synthesis allow robots to adjust their actions flexibly to satisfy given task specifications, optimizing both planning efficiency and strategy effectiveness [20]–[22]. However, these approaches are generally limited to finite time horizons, whereas real-world robotic applications often involve tasks with infinite time horizons. In human-robot interaction scenarios, where robots encounter dynamic disturbances, sampling-based model predictive control approaches, such as Model Predictive Path Integral (MPPI) control [24], effectively handle nonlinearities and nonconvexities by sampling control inputs and simulating system dynamics to approximate optimal control strategies [25], [26] that ensure both interaction safety.

Motivated by the discussion above, this work aims to develop a reactive task and motion planning framework for experimental scenario that can enable plan adjustments, ensure human operator safety and accommodate unexpected task variations in real time. The contributions are summarized as follows. First, a temporal logic-based planning approach, incorporating a planning decision tree and an augmented planning decision tree search method, is developed to dynamically adjust task sequences in response to changes in local temporary tasks and task-related objects during human-robot

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interaction. This approach is particularly effective in handling scenarios where global and local tasks are interdependent. Second, a hierarchical framework is proposed to coordinate the task planning and execution layers, ensuring both the safety of human-robot interaction and strict adherence to task specifications. Third, the effectiveness of the proposed method is validated through physical experiments.

## II. PRELIMINARIES

LTL is a formal language capable of expressing rich task specifications. Given the atomic propositions  $AP$ , the syntax of the LTL formula is defined as

$$\phi := \text{true} \mid ap \mid \phi_1 \wedge \phi_2 \mid \neg\phi_1 \mid X\phi \mid \phi_1 U \phi_2,$$

where  $\text{true}$  is the Boolean value,  $ap \in AP$  is an atomic proposition,  $\phi$  is an LTL formula,  $\neg$  (negation) and  $\wedge$  (conjunction) are standard Boolean operators, and  $X$  (next) and  $U$  (until) are temporal operators. Any LTL formula can be converted to a Nondeterministic Büchi Automata (NBA).

**Definition 1.** An NBA is a tuple  $B = (S, S_0, \Sigma, \rightarrow_B, S_F)$ , where  $S$  is a finite set of states,  $S_0 \subseteq S$  is the initial states,  $\Sigma = 2^{AP}$  is the finite alphabet,  $\rightarrow_B \subseteq S \times 2^\Sigma \times S$  is the state transition, and  $S_F \subseteq S$  is the set of accepting states.

The word  $\pi = \pi_0\pi_1\dots$  is an infinite sequence where  $\pi_i \in 2^{AP}$ ,  $\forall i \in \mathbb{Z}_{\geq 0}$ , with  $2^{AP}$  representing the power set of  $AP$ . Let  $\Delta : S \times S \rightarrow 2^\Sigma$  denote the set of atomic propositions that enables state transitions in NBA, i.e.,  $\forall \pi \in \Delta(s, s'), s \xrightarrow{\pi} s'$ . Then, the NBA can also be defined as  $B = (S, S_0, \Sigma, \Delta, S_F)$ . A run  $s = s_0s_1s_2\dots$  of  $B$  generated by the word  $\pi$  is called valid, if  $s_{i-1} \xrightarrow{\pi_i} s_i, \forall i \in \mathbb{N}_{\geq 1}$ , and  $s$  intersects with  $S_F$  infinitely many times. Co-safe LTL is a special case of LTL, where its satisfaction is defined by a finite sequence of word. More details on LTL syntax, semantics, and model checking can be found in [27]. In this work, we consider a global LTL task  $\Phi_G$  and a temporary local task  $\Phi_L$ , whose corresponding NBA is  $B_G = (S_G, S_{G0}, \Sigma_G, \Delta_G, F_G)$  and  $B_L = (S_L, S_{L0}, \Sigma_L, \Delta_L, F_L)$ , respectively. Since Co-safe LTL is suitable to describe finite length robotic tasks, the local temporary tasks  $\Phi_L$  are specified by co-safe LTL formulas. Let  $\mathbb{Z}_{\geq 0}$ ,  $\mathbb{N}$ ,  $\mathbb{R}^+$ , and  $[N]$  denote the set of non-negative integers, the set of natural numbers, the set of positive real numbers, and the shorthand notation for  $\{1, \dots, N\}$ , respectively. Given a set  $A$ , denote by  $|A|$  the cardinality of  $A$ .

## III. PROBLEM FORMULATION

The state space of the robot, denoted as  $P \subset \mathbb{R}^7$ , represents the pose state of the robot's end-effector. Specifically, a state  $p \in P$  is defined as  $p = [x, y, z, q_w, q_x, q_y, q_z]^T$  where  $x, y, z$  are the Cartesian coordinates of the position, and  $q_w, q_x, q_y, q_z$  are the components of the unit quaternion representing the orientation. Consider a  $n$  DoFs robot manipulator with  $K$  rigid links operating in a bounded workspace  $M \subset \mathbb{R}^3$  containing  $\{m_i\}_{i=1, \dots, n}$  regions of interest (e.g., cuboid regions) associated with the robot state space  $P$ . We denote by  $L_{pm} : P \rightarrow M$  a label function, which

establishes a one-to-one correspondence between an robot's state  $p_i \in P$  and a region of interest  $m_i$ . Let  $O$  be the set of observed objects, where  $o_i \in O$  represents the  $i$ th object. Let  $L_{mo} : M \times O \rightarrow \{0, 1\}$  be a Boolean indicator function that indicates whether an object  $o_i$  is in a region  $m_i$ . The robot configuration is defined as  $x \in \mathbb{R}^n$ . Each link has a rigidly attached coordinate system  $\{S_k\}_{k=1}^K$ , with  $S_0$  as the base frame. The homogeneous transformation matrix  $\mathbf{T}_k \in SE(3)$ , mapping the base frame  $S_0$  to the frame  $S_k$  of the  $k$ -th link, is computed using Denavit-Hartenberg (DH) parameters and joint configuration  $x$  as part of the forward kinematics :  $\mathbf{T}_k = \text{FK}_k(x)$ . To facilitate robot tasks and motion planning, the following transition system is defined.

**Definition 2.** The transition system (TS) is a tuple  $\mathcal{T} = (P, p_0, \rightarrow_{\mathcal{T}}, AP, L, L_M, C_{\mathcal{T}S})$ , where  $P$  is a set of pose states;  $p_0 \in P$  is the initial state;  $\rightarrow_{\mathcal{T}} \subseteq P \times P$  indicates the state transition such that  $(p, p') \in \rightarrow_{\mathcal{T}}$  if the transition is feasible;  $AP$  is the set of atomic propositions (i.e. reaching a specified location or completing a desired task);  $L : P \rightarrow AP$  is a labeling function that indicates the atomic proposition  $ap \in AP$  at the state  $p$ ,  $L_M : AP \rightarrow M$  indicates the interested region associated with the atomic proposition; and  $C_{\mathcal{T}S} : (\rightarrow_{\mathcal{T}}) \rightarrow \mathbb{R}^+$  is the cost of transition, (i.e. the Cartesian distance between states  $p$  and  $p'$ ). Assuming that the path between  $p$  and  $p'$  consists of discrete points  $\gamma_i \in \mathbb{R}^3, i = 1, \dots, n$ , corresponding to the robot's Cartesian positions, the transition cost is defined as  $C_{\mathcal{T}S}(p, p') = \sum_{k=1}^{n-1} \|\gamma_{k+1} - \gamma_k\|, \forall (p, p') \in \rightarrow_{\mathcal{T}}$ .

The plan of global task  $\Pi$  is defined as  $\Pi = (s_G, p, \pi)$ , where  $s_G = s_0^G s_1^G s_2^G \dots$  is the sequence of states of  $B_G$ ,  $p$  represents the sequence of states, and  $\pi$  is the word defined before. By [27], the plan  $\Pi$  can be written in the form of prefix-suffix structure  $\Pi = \Pi_{pre}[\Pi_{suf}]^w$ , where  $\Pi_{pre}$  is the prefix part starting from an initial state and ending at an accepting state and  $\Pi_{suf}$  is the suffix part with the same starting and ending NBA state. There exists  $\pi_i \in \Delta_G(s_{i-1}^G, s_i^G), \forall i \in [|\Pi|]$ , and  $s_{|\Pi_{pre}|}^G = s_{|\Pi_{suf}|}^G \in F_G$ . The cost of plan  $p$  is defined as  $J(p) = \sum \|p - p'\|, \forall (p, p') \in \rightarrow_{\mathcal{T}}$ . Consequently, the cost of a prefix-suffix plan  $\Pi$  can be defined as  $J(p) = wJ(p^{pre}) + (1 - w)J(p^{suf})$  [7], where  $w$  is the tuning weight. Given a local task  $\Phi_L$ , the local plan is defined as  $\Pi_{tem} = (s_G, s_L, p, \pi)$ , where  $s_L = s_0^L s_1^L s_2^L \dots$  is the sequence of states of  $B_L$ . When a temporary task  $\Phi_L$  is activated,  $\Pi$  should satisfy  $\Phi_L$  while respecting  $\Phi_G$ . A temporal plan satisfies both  $\Phi_G$  and  $\Phi_L$  if,  $\forall i \in [n], \pi_i \in \Delta_L(s_{i-1}^L, s_i^L), \pi_i \in \Delta_G(s_{i-1}^G, s_i^G)$  and  $s_n^L \in F_L$ , which is denoted as  $\Pi_{tem} \models (\Phi_G, \Phi_L)$ .

**Assumption 1.** There exists a plan  $\Pi$  satisfying task  $\Phi_G$  and  $\Phi_L$  during human-robot interactions.

**Problem 1.** Given global task  $\Phi_G$  and local temporary task  $\Phi_L$ , the goal is to design a real-time reactive framework that can determine and execute an infinite sequence  $x$  that minimizes  $J(p)$  while ensuring: (1) the completion of  $\Phi_G$ ; (2) the completion of local temporary task  $\Phi_L$  while not violating  $\Phi_G$ ; (3) avoiding collision and adjusting plan  $\Pi$

during human-robot interaction .

#### IV. REACTIVE PLANNING FOR SAFE HUMAN-ROBOT INTERACTION

This section introduces a real-time reactive planning framework designed to accommodate environmental and task variations in human-robot interactions while ensuring an optimal and safe path  $p$ . As illustrated in Fig. 1, the *task planner* manages both the global task  $\Phi_G$  and the local task  $\Phi_L$ , transforming them into their corresponding NBA representations  $B_G$  and  $B_L$ . An initial offline and optimal task plan  $\Pi$  is then generated using a planning decision tree search. To handle temporary tasks and dynamic environmental changes, we further develop an augmented planning decision tree along with *motion generator* to enable rapid real-time adaptation of  $p$  while ensuring collision-free motion. The *planning interface* coordinates the planning and execution layer, ensuring adherence to task constraints.

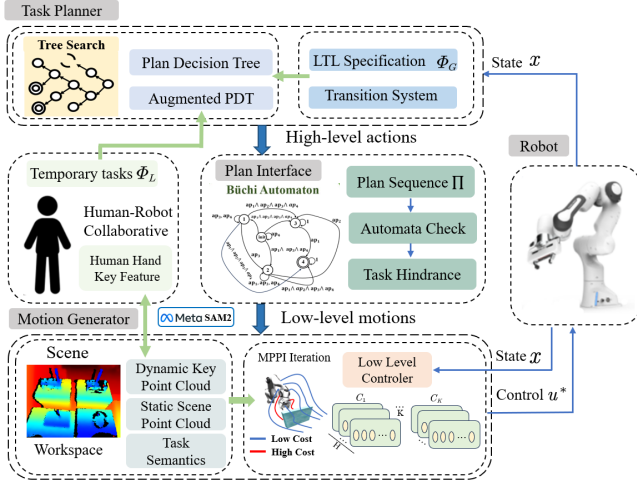


Fig. 1: The framework of real-time reactive planning.

##### A. Task Planner

To obtain an optimal task plan  $\Pi$  that satisfies  $\Phi_G$  in real time, inspired by previous work [11], we construct a planning decision tree to represent the task progress and expand nodes that align with automaton transitions. This approach restricts the search to relevant automaton states and sub-tasks, thereby avoiding constructing and traversing the product automaton.

**Definition 3.** The planning decision tree  $\mathcal{T}_P$  is constructed based on a set of nodes  $\{d_i^P\}$ ,  $i \in \mathbb{Z}_{\geq 0}$ , where  $d_0^P$  represents the root, and each node in  $\mathcal{T}_P$  is defined as a tuple

$$d_i^P = (s_i, p_i, ap_i, \text{Ori}(d_i^P), \text{Tra}(d_i^P), C(d_i^P), \text{Flag}(d_i^P))$$

where  $s_i \in S$  denotes the automaton state,  $p_i \in P$  denotes the robot pose state,  $ap_i \in AP$  denotes the atomic proposition,  $\text{Ori}(d_i^P)$  denotes the parent node of  $d_i^P$ ,  $\text{Tra}(d_i^P) \in \{0, 1\}$  indicates whether  $d_i^P$  can generate its child nodes and  $\text{Tra}(d_i^P) = 0$  by default,  $C(d_i^P)$  represents the total Cartesian distance. Specifically, for a node sequence  $d_{i_0}^P d_{i_1}^P \dots d_{i_n}^P$ , where  $i_0 = 0$ ,  $i_n = i$ , the cost is defined as  $C(d_i^P) = \sum_{j=1}^n C_{\mathcal{T}\mathcal{S}}(p_{i_j}, p_{i_{j-1}})$ . It is simulated and computed through

sampling method based on GPU acceleration [28]. For the initial static environment,  $C_{\mathcal{T}\mathcal{S}}(p_{i_j}, p_{i_{j-1}})$  will be saved through cache to avoid repeated calculation overhead.

##### Algorithm 1 Planning Decision Tree

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**Input:** Global Task  $\Phi_G$ , Workspace  $M$ , Initial Node  $d_0$   
**Output:**  $\Pi_{pre}, \Pi_{suf}$

- 1: Convert  $\Phi_G$  to NBA  $B_G$ ;
- 2: Initialize the tree  $\mathcal{T}_P = \{d_0^P\}$
- 3: **while** True **do**
- 4:   **if**  $\text{Tra}(d_i^P) = 1, \forall d_i^P \in \mathcal{T}_P$  **then**
- 5:     **break**
- 6:   # Generate Children Node By Tree Expansion
- 7:   **for**  $d_i^P \in \mathcal{T}_P$  s.t.  $\text{Tra}(d_i^P) = 0$  **do**
- 8:     **for**  $s \in S \setminus \text{PreS}(d_i^P)$  **do**
- 9:       **for**  $p$  s.t.  $L(p) \in \Delta(s_i, s) \wedge L_{mo}(L_{pm}(p), o_i)$  **do**
- 10:         Add  $d_{chi}^P$  to  $\{d_{chi}^P\}$  and Update  $\text{PreS}(d_{chi}^P)$
- 11:   # Avoid Unnecessary Expansion By Tree Pruning
- 12:   **for**  $d_{sub}^P$  in  $\{d_{chi}^P\}$  **do**
- 13:     **if**  $\text{Prog}(d_{sub}^P) = \text{oth}$  **then**  $\text{Tra}(d_{sub}^P) = 1$
- 14:     **for**  $d_i^P$  in  $\mathcal{T}_P$  **do**
- 15:       **if**  $s_i = s_{sub}$  and  $\text{Prog}(d_i^P) = \text{Prog}(d_{sub}^P)$  **then**
- 16:         **if**  $C(d_i^P) < C(d_{sub}^P)$  **then**
- 17:          $\text{Tra}(d_{sub}^P) = 1$ ;
- 18:         Delete  $d_{sub}^P$  and all its leaf nodes in  $\mathcal{T}_P$
- 19:     Add  $d_{sub}^P$  to  $\mathcal{T}_P$
- 20:     Set  $\text{Tra}(d_i^P) = 1$
- 21:  $\Pi_{pre}, \Pi_{suf} = \text{Get\_Plan}(\mathcal{T}_P)$
- 22: **Return**  $\Pi_{pre}, \Pi_{suf}$

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Let  $\text{Prog}(d_i^P) \in \{pre, oth\} \cup S_F$  indicate the associated task stage, where *pre* and *oth* represent the prefix stage and the completion of first suffix stage, respectively, and  $s \in S_F$  indicates that the plan is in the suffix stage with starting state  $s$ . The task stage  $\text{Prog}(d_i^P)$  evolves according to

$$\text{Flag}(\text{Prog}(d_i^P), s) = \begin{cases} \text{Prog}(d_i^P), & \text{if } s \notin S_F, \\ s, & \text{if } s \in S_F, \\ \text{oth}, & \text{if } \text{Prog}(d_i^P) = s. \end{cases}$$

Let  $d_{chi}^P$  represent the child node generated by parent node  $d_{par}^P$  and  $\text{PreS}(d_{chi}^P)$  records the automaton states of nodes that share the same mission stage within the  $d_{par}^P$ . The  $\text{PreS}(d_{chi}^P)$  is updated based on  $\text{Prog}(d_{par}^P)$ . If  $\text{Prog}(d_{par}^P)$  changes, we reset  $\text{PreS}(d_{chi}^P) = \emptyset$ . Otherwise,  $\text{PreS}(d_{chi}^P) = \text{PreS}(d_{par}^P) \cup \{s_{chi}\}$ , which avoids the same NBA states appearing in one task stage.

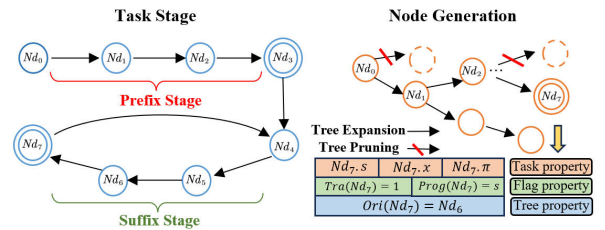


Fig. 2: The task stages of  $\varphi$  and the construction of planning decision tree by Tree Expansion and Tree Pruning.

The planning process is outlined in Alg. 1. As shown in Fig. 2, the tree  $\mathcal{T}_P$  represents the task stages and system states

and generates children nodes incrementally from the initial node  $d_0^P$  including the initial state  $s_0$ , the initial position  $p_0$ , the initial proposition  $ap_0$  with  $\text{Prog}(d_0^P) = \text{pre}$  and  $\text{PreS}(d_0^P) = \{s_0\}$ . If  $d_{chi}^P$  has the same  $s$  and  $\text{Prog}$  with a node  $d_i^P$  in  $\mathcal{T}_P$  and  $C(d_i^P) < C(d_{chi}^P)$ , the  $d_{chi}^P$  will no longer be traversed, and the paths from the  $d_i^P$  to its leaf nodes will all be pruned out from  $\mathcal{T}_P$ . Finally, the function  $\text{Get\_Plan}(\mathcal{T}_P)$  performs backtracking to the root node to obtain the plan sequence  $\Pi \models \Phi_G$ . In offline planning,  $L_{mo}(L_{pm}(p), o_i)$  is set according to the initial state of objects  $o_i$  in the workspace  $M$ .

### B. Reactive Task Plan

During task execution, the robot must satisfy the global task specification  $\Phi_G$  while also addressing local temporary tasks  $\Phi_L$ . This planning process must coordinate the two task requirements and ensure that no task constraints are violated in real-time. We extend the original planning decision tree  $\mathcal{T}_P$  and consider the state transitions of the automata corresponding to the two tasks at the same time. We construct an augmented planning decision tree  $\mathcal{T}_J$  comprising a set of nodes  $\{d_i^J\}$ ,  $i \in \mathbb{Z}_{\geq 0}$  with  $d_0^J$  being the root. Each node  $d_i^J$  is characterized by a tuple  $d_i^J = (p_i, ap_i, s_i^G, s_i^L, C(d_i^J))$ , where  $ap_i \in AP$  and  $p_i \in P$  are the same to  $\mathcal{T}_P$ ,  $s_i^G \in S_G$  denotes the global task state,  $s_i^L \in S_L$  indicates the local task state. Similar to  $C(d_i^P)$ ,  $C(d_i^J)$  is the cost defined on a node sequence. For the node sequence  $d_{i_0}^J d_{i_1}^J \dots d_{i_n}^J$ , where  $i_0 = 0$  and  $i_n = i$ , the cost is defined as  $C(d_i^J) = \sum_{j=1}^n C_{\mathcal{T}_S}(p_{i_j}, p_{i_{j-1}})$ . A transition  $(d_i^J, d_j^J) \in E$  is considered feasible if it satisfies both the local task  $\Phi_L$  and the global task  $\Phi_G$ . This is achieved when  $ap_j \in \Delta_L(s_i^L, s_j^L)$  or  $ap_j \notin AP_L$ , and  $ap_j \in \Delta_G(s_i^G, s_j^G)$  or  $ap_j \notin AP_G$ .

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### Algorithm 2 Augmented Planning Decision Tree

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**Input:** Global Task  $\Phi_G$ , Local Task  $\Phi_L$ ,  $AP$

**Output:**  $\Pi_{tem}, \Pi_{pre}, \Pi_{suf}$

- 1: Convert  $\Phi_G, \Phi_L$  to NBA  $B_L, B_G$ ;
- 2: Initialize the tree  $\mathcal{T}_J = \{d_0^J\}$
- 3: **for**  $i = 1$  **to**  $step_{max}$  **do**
- 4:  $d_j^J = \text{Sample}(\{d_i^J\})$ ,  $s_i^L = s_j^L$ ,  $s_i^G = s_j^G$
- 5:  $ap_i = \text{Sample}(AP)$
- 6: **if**  $ap_i \in \Delta_L(s_j^L, s_i^L)$  **then**  $s_i^L = \text{Sample}(S_i^L)$ ;
- 7: **if**  $ap_i \in \Delta_G(s_j^G, s_i^G)$  **then**  $s_i^G = \text{Sample}(S_i^G)$ ;
- 8: **if**  $L_{mo}(L_{pm}(p_i), o_i)$  **then**
- 9:     **Add**  $(d_j^J, d_i^J)$  **into**  $\text{Edge } E$ ;
- 10:      $C(d_i^J) = C(d_j^J) + C_{\mathcal{T}_S}(d_i^J.p_i, d_j^J.p_j)$ ;
- 11:     **# Pruning to avoid invalid states search**
- 12:     **for**  $(d_j^J, d_i^J)$  in  $E$  **and**  $(d_j^J, d_i^J)$  is feasible **do**
- 13:         **if**  $d_i^J \equiv d_j^J$  **and**  $C(d_i^J) \leq C(d_j^J)$  **then**
- 14:             Delete  $d_j^J$  from  $\{d_i^J\}$
- 15:             **for**  $d_k^J$  in  $\{d_i^J\}$
- 16:                 **if**  $C(d_i^J) - C(d_k^J) > C_{\mathcal{T}_S}(d_i^J.p_i, d_k^J.p_k)$  **then**
- 17:                     Delete  $(d_j^J, d_i^J)$  from  $E$ , Add  $(d_k^J, d_i^J)$  to  $E$
- 18:                      $C(d_i^J) = C(d_k^J) + C_{\mathcal{T}_S}(d_i^J.p_i, d_k^J.p_k)$
- 19: Get  $d_{min}^J$ , s.t.  $s_{min}^L \in F_L$  and  $s_{min}^G$  is reachable to  $F_G$ ;
- 20: Obtain  $\Pi_{tem}$  from  $d_0^J$  to  $d_{min}^J$  according to  $E$ ;
- 21: Initial root node  $N = \{d_0^J\} = (ap_{min}, s_{min}^G)$ ;
- 22:  $[\Pi_{pre}, \Pi_{suf}] = \text{Planning Decision Tree}(\Phi_G, \{d_{min}^J\})$ ;
- 23: **return**  $\Pi_{tem}, \Pi_{pre}, \Pi_{suf}$ ;

The augmented planning decision tree search based on  $\mathcal{T}_J$  is outlined in Alg. 2, which achieves efficient local task planning by sampling atomic propositions  $AP$  and iterating through the states of automata  $B_G$  and  $B_L$ . This approach prunes nodes during the tree expansion process, avoiding the expansion of invalid states. After constructing the tree  $\mathcal{T}_J$ , the node  $d_{min}^J$  with the minimum  $C(d_{min}^J)$  and also satisfy minimizes  $J(p)$  is selected among those completing the local task  $\Phi_L$  and global task  $\Phi_G$ . For the corresponding state  $s_{min}^G$ , there exists a finite sequence of transitions  $\Pi$  and states  $s = s_{min}^G, \dots, s_n^G$ , where  $i$  is the index of the states, such that  $\pi_i \in \Delta(s_{i-1}, s_i)$  for all  $i$ , and  $s_n^G \in F_G$ , ensuring consistency between local and global task completion.

### C. Motion Generator

To enable reactive motion planning during human-robot interaction, accurately estimating the distance between robot, workspace and human operator is crucial. Specifically, the robot's workspace is represented as a dense set of points  $\{\mathbf{o}_m \in \mathbb{R}^3\}_{m=1, \dots, O}$ . Given a set of robot configurations  $\{x_i\} \in X$ , following the works of [25], a batch of  $N$  control points  $\{\mathbf{k}_j(x) \in \mathbb{R}^3\}_{j=1, \dots, N}$  can be obtained for each configuration  $x$  by forward kinematics. The Configuration Signed Distance Function (CSDF) [29] is then employed,

$$\text{CSDF}(x) := \min_{j=1, \dots, N} \left( \min_{m=1, \dots, O} \|\mathbf{k}_j(x) - \mathbf{o}_m\| \right) - r, \quad (1)$$

where  $r$  represents a safety threshold. Positive CSDF indicates that the robot is safe and away from obstacles.

Model Predictive Path Integral (MPPI) is based on a discrete-time, continuous-state system:  $x_{t+1} = x_t + e_t$  with  $e_t \sim \mathcal{N}(d_t, \Sigma)$ , where  $\mathcal{N}(d_t, \Sigma)$  denotes a multivariate Gaussian distribution with mean  $d_t$  representing the nominal displacement from  $x_t$  at time  $t$  and covariance matrix  $\Sigma$ . We begin the MPPI loop by assuming a straight-line path between the initial and target configurations. The path is discretized into intermediate waypoints, and the corresponding nominal displacements are calculated to serve as the initial conditions for MPPI updates. At each MPPI iteration,  $Z$  candidate sequences of displacements  $E_i = \{e_{i,h}\}_{h=0}^{H-1}$ ,  $i = 1, \dots, Z$ , are sampled from  $\mathcal{N}(d_t, \Sigma)$  based on a series of nominal configurations trajectory  $x_0, \dots, x_H$ , and corresponding nominal displacements  $d_0, \dots, d_{H-1}$  over a control horizon  $H$ . The sampling and evaluation processes are using GPU. The rollout cost  $C(E_i)$  is the weighted sum of  $C_{\text{terminal}}$  and  $C_{\text{run}}$ . Specifically, the terminal cost

$$C_{\text{terminal}}(E_i) := w_{\text{terminal}} \|x_{i,H} - x_{\text{goal}}\| \quad (2)$$

quantifies the distance between the actual configuration at the end of the rollout and the goal configuration, where  $w_{\text{terminal}}$  is the tuning weight. For the running cost  $C_{\text{run}}$ , we consider weighted contributions from the total path length, collisions with the external environment, self-collisions, and the avoidance of stagnation. The running cost is defined as

$$C_{\text{run}}(E_i) = C^{\text{length}}(E_i) + C^{\text{coll}}(E_i) + C^{\text{self-coll}}(E_i) + C^{\text{stay}}(E_i) \quad (3)$$

$$C^{\text{length}}(E_i) := w_{\text{length}} \sum_{t=0}^{H-1} \|\text{FK}_K(x_{i,t} + e_{i,t}) - \text{FK}_K(x_{i,t})\|, \quad (4)$$

$$C^{\text{coll}}(E_i) := w_{\text{coll}} \sum_{t=0}^{H-1} c_{\text{coll}}(x_{i,t}, e_{i,t}), \quad (5)$$

$$C^{\text{self-coll}}(E_i) := w_{\text{self-coll}} \sum_{t=0}^{H-1} c_{\text{self-coll}}(x_{i,t}, e_{i,t}), \quad (6)$$

$$C^{\text{stay}}(E_i) := w_{\text{stay}} \frac{C^{\text{terminal}}(E_i)}{\max(\epsilon, \|x_{i,1} - x_{i,H}\|_2)}, \quad (7)$$

where  $w_{\text{length}}$ ,  $w_{\text{coll}}$ ,  $w_{\text{self-coll}}$ ,  $w_{\text{stay}}$  are the tuning weights.  $C^{\text{length}}(E_i)$  is to penalize long movement distance of the end effector in Cartesian space. In (5),  $c_{\text{coll}}$  is designed as

$$c_{\text{coll}}(x_{i,t}, e_{i,t}) := \begin{cases} 1 & \text{if CSDF}(x_{i,t}) \leq \delta, \\ \frac{\delta}{\text{CSDF}(x_{i,t})} & \text{if CSDF}(x_{i,t}) > \delta, \end{cases} \quad (8)$$

where the cost is set to 1 if the CSDF is below the threshold  $\delta$  and decreases as CSDF rises. In (6),  $c_{\text{self-coll}}$  is estimated through neural network as in [26]. In (7),  $C^{\text{stay}}$  penalizes static trajectories, encouraging exploration, reducing being stuck far from the goal. When trajectory converges to  $x_{\text{goal}}$ , this cost becomes zero. The cost of trajectory  $E_i$  is defined as  $S(E_i) = C(E_i) + \lambda \sum_{t=0}^{H-1} d_t^\top \Sigma^{-1} e_{j,t}$ . The exponential averaging  $\Omega(E_i)$  is defined as

$$\Omega(E_i) := \exp\left(-\frac{1}{\lambda} \left(S(E_i) - \min_{i=1, \dots, Z} S(E_i)\right)\right), \quad (9)$$

where  $\lambda$  is the temperature parameter influencing its exploration performance. The nominal displacements are then updated based on the exponential averaging of the rollout costs and a weighted sum of  $\Omega(E_i)$ . Specifically, at the  $i$ th iteration, the nominal distance  $d_t$  is updated according to

$$d_t := (1 - \alpha_d) d_{t-1} + \alpha_d \cdot \frac{\sum_{i=1}^Z \Omega(E_i) \cdot e_{i,t}}{\sum_{i=1}^Z \Omega(E_i)}, \quad (10)$$

where  $\alpha_d \in (0, 1)$  is a tunable weight influencing the smoothness of the control input generation.

Given a set of discrete configurations trajectory  $x$  from the current configuration  $x$  to  $x_{\text{goal}}$ ,  $x_{s^*}$  is identified as the farthest configuration from  $x$  that is still within a safe distance. Specifically,  $x_{s^*}$  is selected as

$$x_{s^*} := \arg \max_{x_i} \{\|x - x_i\| \mid \|\mathbf{k}(x_i) - \mathbf{k}(x)\| \leq \text{CSDF}(x)\}. \quad (11)$$

Once the goal configuration  $x_{s^*}$  is determined, a potential field for trajectory following is constructed following [25] as

$$\varphi(x) := \frac{\|x - x_{s^*}\|^2 + \epsilon}{\text{CSDF}(x) + \epsilon}, \quad (12)$$

where  $\epsilon$  denotes a small constant that ensures numerical stability. Finally, the control input is designed along the gradient of the potential field as

$$u(x) := -k \nabla \varphi(x), \quad (13)$$

where  $k$  is a positive weight. By employing rolling optimization to determine the control input  $u$  and applying it to the robot, safe motion can be achieved. In human-robot interaction, the influence of the human is modeled as a dynamic point cloud which generated by dynamically tracking the human hand's mask [30] and integrated into the workspace point cloud to generate control sequence, ensuring safety during the human-robot interaction process.

The planning interface restricts the planning domain according to the high-level task sequence, ensuring task constraints are satisfied. In the process of motion generation, atomic proposition  $ap$  corresponding Cartesian regions  $L_M(ap)$  that are restricted during the task transition must be treated as static obstacles and incorporated into the low-level controller. To this end, the hindrance in  $\Pi$  are defined as  $HIN = hin_0 hin_1, \dots$ , where  $hin_i \in 2^{AP}$  for  $i = 0, 1, \dots$ , indicating the banned actions and associated areas during the transition from  $\Pi_i$  to  $\Pi_{i+1}$ . Specifically, the hindrance set  $HIN$  is constructed by identifying constraints during state transitions in the plan  $\Pi$ . For each state  $\Pi_i = (s_i, x_i, \pi_i)$ , the prohibited action  $ap \in AP$  during the transition from  $s_{i-1}$  to  $s_i$  will be checked by Alg. 3. If  $\pi_i \wedge ap$  is not in the transition set  $\Delta(s_{i-1}, s_i)$ , such actions are added to  $hin_i$  to ensure no prohibited actions occur. During the execution of  $\Pi_i \rightarrow \Pi_{i+1}$ , the transitions from  $p_i$  to  $p_{i+1}$  with  $L_M(hin_i)$  as a static obstacle in MPPI planning ensures that the task constraints are met. When human-robot interaction exceeds the threshold time or causes changes in  $L_{mo}(m_i, o_i)$ , new control sequence  $u$  will be generated by combining algorithms 1, 2, and 3 to satisfy the minimization of  $J(p)$ .

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### Algorithm 3 Low-level Motion planning

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**Input:** Plan  $\Pi$ , Büchi Automata  $B$

**Output:** Hindrance Set  $HIN$ , Set of Control Inputs  $u$

- 1: Initialize  $HIN \leftarrow \emptyset$ ;
  - 2: **for** each state  $\Pi_i = (s_i, p_i, \pi_i)$  **do**
  - 3:   **if**  $ap$  is prohibited in transition  $s_{i-1} \rightarrow s_i$  **then**
  - 4:     **if**  $\pi_i \wedge ap \notin \Delta(s_{i-1}, s_i)$  **then**
  - 5:       Add  $ap$  to hindrance  $hin_i$ ;
  - 6:     Compile  $hin_i$  into  $HIN$ ;
  - 7: **for** each plan  $\Pi_i \rightarrow \Pi_{i+1}$  **do**
  - 8:   **if**  $L(p_i)$  in  $HIN$  **then**
  - 9:     Add  $L_M(hin_i)$  and Remove  $L_M(ap_i)$
  - 10:   **else**
  - 11:     Add  $L_M(hin_i)$  as static obstacle;
  - 12:    Get minimum norm solution  $x_{i+1}$  from  $(x_i, p_i)$ ;
  - 13:    Generate the control input  $u$  by motion generator
  - 14: **return**  $HIN, u$ ;
- 

## V. EXPERIMENT

Consider a human-robot interaction scenario in chemical experimentation. The robot is responsible for sequentially performing tasks such as sampling, dispensing, and stirring within designated areas according to the experimental protocol. Additionally, the robot must handle unexpected sampling tasks while ensuring that these actions do not conflict with the overall experimental protocol. Compared with the related methods in Table I, our method can handle local tasks with complex and long-sequence task specifications. When

Method	Dynamic Scenario	Online Coordination			Product Automaton Free <sup>1</sup>	Inheritance Task Progress <sup>2</sup>
		Local Long Task	Local Single Task	Coupled Local Task		
Vasile [12]	✓	✗	✓	✗	✗	✓
Kantaros [13]	✓	✗	✓	✗	✓	✓
Finkbeiner [14]	✗	✓	✓	✗	✗	✓
Li [15]	✗	✗	✓	✗	✗	✓
Sahin [16]	✗	✗	✗	✗	✓	✗
Kurtz [17]	✗	✗	✗	✗	✓	✗
Ours	✓	✓	✓	✓	✓	✓

TABLE I: Comparison with Related Literature.

<sup>1</sup> Product Automaton Free means that there is no need for explicit product of transition system and automaton, which can reduce the search space.

<sup>2</sup> Inheritance Task Progress means that the current task progress can be preserved, and there is no need to start the search from scratch.

local tasks are coupled with global tasks, our method can coordinate the two types of tasks and ensure that both task specifications are strictly followed.

The global tasks  $\Phi_G$  are represented by atomic propositions  $ap_i$ ,  $i = 1, \dots, 6$ , which correspond to the actions: taking a sample tube in Area 1 or Area 2, dispensing the sample in Area 3, placing the test tube in Area 1 or Area 2, picking up the stirring rod in Area 4, using the stirring rod to stir in Area 3, and placing the stirring rod back in Area 4, respectively. Initially, Alg. 1 is used to generate the offline task planning:

$$\Phi_G = G \left( \left( \bigwedge_{i=1}^5 (ap_i \rightarrow Xap_{i+1}) \right) \wedge (ap_6 \rightarrow Fap_1) \right) \wedge Fap_1$$

The local (temporary) tasks are specified via co-safe LTL as

$$\Phi_L = \bigwedge_{i=7,8,9} (\neg(ap_{i+1})U(ap_i \wedge \neg ap_{i+1})) \wedge Fap_{10},$$

where  $ap_7$  and  $ap_9$  represent the task of placing pill A or B in Area 3, and  $ap_8$  and  $ap_{10}$  represent picking up pill A from Area 6 and pill B from Area 5, respectively. During the process of chemical experimentation,  $\Phi_L$  can be triggered by the operator anytime based on the experiment's progress.

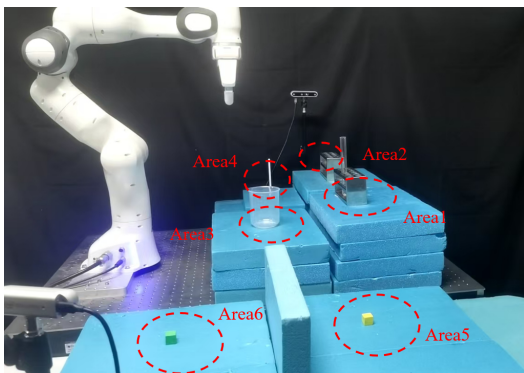


Fig. 3: The experimental setup, where each region corresponds to a different operation task.

In the experiment, we utilize a Franka Panda with NVIDIA RTX-3060. RealSense D455 and D435 RGB-D cameras are in an eye-to-hand setup to track the operator's hand point cloud [30] and monitor the spatial distribution of

environmental objects [31]. Spacemouse is used as a trigger for local tasks. LTL2BA [32] is used to convert LTL formulas into Büchi automata. To perform  $\Phi_G$ , by Alg. 1,  $\Pi_{pre} = ap_0ap_1$  and  $\Pi_{suf} = ap_2ap_3ap_4ap_5ap_6ap_1$  are generated offline within 0.14s. The local task  $\Phi_L$  is then triggered by the operator in Fig. 4. For all  $p_i$ ,  $i \in \{1, \dots, j\}$ , each term  $C_{TS}(p_0, p_i)$  is updated by Curobo [28] within 1.8s. By Alg. 2, the task plan is updated to  $\Pi_{tem}\Pi_{pre} = ap_{10}ap_9ap_8ap_7ap_4$  and  $\Pi_{suf} = ap_5ap_6ap_1ap_2ap_3ap_4$  within 0.27s based on its current task state. To avoid task conflicts, Alg. 3 is used to generate the set  $HIN = \{\{ap_7, ap_8, ap_9\}, \{ap_7, ap_8\}, \{ap_7\}, \{\emptyset\}\}$  according to  $\Pi_{tem}$ , which treats the cuboid region corresponding to  $L_M(ap)$  as a static obstacle when generating the control sequences. When the label  $L_{mo}(m_i, o_i)$  in the environment changes during human-robot interaction, reactive planning will be performed to regenerate the path sequence  $p$  that meets the task specifications. During the interaction process, the operator's safety and the strict execution of the task specifications are guaranteed.

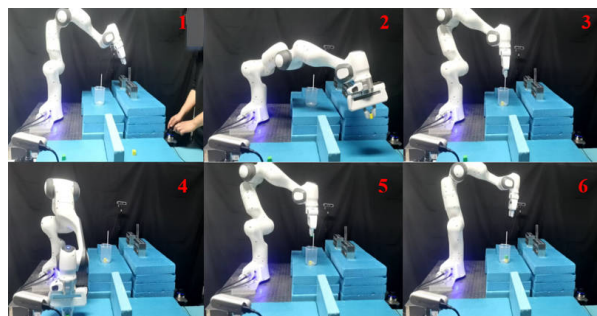


Fig. 4: The snapshots of local tasks. When the operator triggers a temporary task for the robot, the robot is able to record the current state of the global task and execute the temporary task without violating the global task constraints.

## VI. CONCLUSIONS

This work develops a real-time motion planning framework that ensures the safety of human-robot interaction and enables the robot to follow a globally planned LTL task while responding to local temporary tasks. Future work will consider timed temporal logic constraints and integrate

human intent recognition mechanisms to better predict and adapt to human actions in real-time.

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